## Pascall's Triangle and the Binomial Theorem (8 pers)

Mathematics 1 Outcome 1a

Pd	Lesson, Outline, Approach etc.	Nelson MIA - AH M1	TeeJay Publishers
1	Introduction to Pascal's Triangle via routes along a set of	$(2x+1)^5$ , $(4x-1)^3$ ,	$(x+5)^{6}, (x+\frac{1}{x})^{4},$
	roads leading to $(a + b)^n n = 1, 2, 3,$	$(2x-\frac{1}{x})^5$ , $(3x^2+1)^6$ .	etc + Pg3, Ex1, Qu2
2	Define n! = n(n-1)(n-2)3.2.1 (calculator)		
	Define ${}^{n}C_{r}$ as choosing <i>r</i> from <i>n</i> ;	Pge 7, Ex 2B Qu 1a, 2, 4a,b	
	${}^{n}\mathcal{C}_{r} = \binom{n}{r} = \frac{n!}{n!(n-r)!};$	5a, 6a, 7a,b (d)	
	Show quick way of finding :-		
	$ \begin{pmatrix} 10\\3 \end{pmatrix} = \frac{10!}{3!7!} = \frac{10 \times 9 \times 8}{3 \times 2 \times 1} \times \left( \frac{7 \times 6 \times 5 \times 4 \times 3 \times 2 \times 1}{7 \times 6 \times 5 \times 4 \times 3 \times 2 \times 1} \right) = 120 $		
	Go over $\binom{n}{r} = \binom{n}{n-r}$ ; and		
	$\binom{n}{r-1} + \binom{n}{r} = \binom{n+1}{r}$		
3	Look at $\begin{pmatrix} 4 \\ 0 \end{pmatrix} = 1$ , $\begin{pmatrix} 4 \\ 1 \end{pmatrix} = 4$ , $\begin{pmatrix} 4 \\ 2 \end{pmatrix} = 6$ , $\begin{pmatrix} 4 \\ 3 \end{pmatrix} = 4$ , $\begin{pmatrix} 4 \\ 4 \end{pmatrix} = 1$ and	Pge 9, Ex 3A Qu 1a-d	Pge 5, Ex 2, Qu 1
	compare with Pascal's triangle.	2a(ı), (III), & b	
	$\Rightarrow (a+b)^{n} = {\binom{n}{0}}a^{n} + {\binom{n}{1}}a^{n-1}b^{1} + {\binom{n}{2}}a^{n-2}b^{2} + \dots + {\binom{n}{n}}b^{n}$		
4	Expand $(1 + 2x - 3x^2)^5$ up to term in $x^3$	$(1 - x + x^2)^6$ up to $x^3$ , $x^3$ , $(x^2 + 4x + 1)^7$ up	$(2 + x - 3x^2)^5$ up to to $x^2$
5	Define General term $T_{r+1} = {n \choose r} a^{n-r} b^r$ and its importance	Pge 9, Ex 3A Qu 3a-d, 4f	
	in finding particular terms like the term in $x^7$ in $(3+2x)^{12}$		
	or the term independent of x in $\left(2x + \frac{1}{x}\right)^{10}$		
6	Show how to find term in $x^3$ in expn of $(1 + 3x - 2x^3)(1 + 2x)^7$ Use "Rainbows"	Pge 11, Ex 3B Qu 1a, c, 4a,b, 5a, 6	
7	Obtain (0.97) <sup>6</sup> correct to 3 decimal places	Pge 13, Ex 4 Qu 1	Pge 5, Ex2 Qu 2-4(b)
8	Checkup and Round-up		
	Cumulative total = 8 periods		



### Partial Fractions (4/5 periods)

#### Mathematics 1 Outcome 1b

Pd	Lesson, Outline, Approach etc.	Nelson MIA - AH M1	TeeJay Publishers
1	Define Rational Function as $f(x) = \frac{P(x)}{Q(x)}$ where P(x) and $Q(x)$ are polynomials and show that $\frac{1}{x+1} + \frac{3}{x-2} = \frac{4x+1}{(x+1)(x-2)} \Rightarrow$ in reverse $\frac{4x+1}{(x+1)(x-2)} = \frac{1}{x+1} + \frac{3}{x-2}$ (Partial Fractions)	Pge 18 Ex 2 Qu 1, 5, 12, 18, 19 22, 25	Page 7 Ex 1 Qu 1a, b, c
2	Deal with repeated fractions in denominator :- $\frac{x^2 - 7x + 9}{(x+2)(x-1)^2} = \frac{A}{x+2} + \frac{B}{x-1} + \frac{C}{(x-1)^2}$ etc.	Pge 19 Ex 3 Qu 1, 3, 5, 10 14, 18	Pge 8 Ex 2
3	Deal with irreducible quadratic factor in denominator:- $\frac{3x^2 + 2x + 1}{(x+1)(x^2 + 2x + 2)} = \frac{A}{x+1} + \frac{Bx + C}{x^2 + 2x + 2}$ etc.	Pge 20 Ex 4 Qu 1, 5, 7, 9, 11* * needs polyl rem theorem	Pge 9 Ex 3
4	Go over need to "divide out" if degree of numerator is greater than or equal to that of denominator :- $\frac{x^3 + 4x^2 - x + 2}{x^2 + x} = x + 3 + \frac{2}{x} - \frac{6}{x + 1} \text{ etc}$ ([A/B]	Pge 22 Ex 6 Qu 1a, b, e, j, l	
5	Review		
	Cumulative total = 13 periods		



### Differential Calculus (8/9 pers)

Mathematics 1 Outcome 2a

Pd	Lesson, Outline, Approach etc.	Nelson MIA - AH M1	TeeJay Publishers
1	First Principals => $f'(x) = \lim_{h \to 0} \frac{f(x+h) - f(x)}{h}$ Go over finding $f'(x)$ for $f(x) = 4x^2$ , $x^3 + 2$ , $\frac{5}{x}$ etc (Not tested formally, but should understand)	Page 29 Ex 1A Qu 1, 4, 5, 7	Page 11, Ex 1
2.	Go over basic S5 rules for differentiation and show importance of "chain rule"	Page 32 Ex 3A Qu 1a,d 2a,c,d 3a, 4a, 6a	Page 12 Ex 2 Page 13 Ex 3
3.	Introduce "Product Rule"	Page 32 Ex 4A Qu 1, 2b, 3 Page 36 Ex 4B Qu 1b, 3, 4	Page 14 Ex 4
4.	Introduce "Quotient Rule"	Page 37 Ex 5A Qu 1, 2, 3, 4, 6 Page 38 Ex 5B Qu 1 - 3	Page 15 Ex 5
5	Define secant $\theta$ = sec $\theta$ = $\frac{c}{b} = \frac{1}{\cos\theta}$ etc. use Graphics calcr to sketch graphs of sec $\theta$ Look at simple properties => $ \sec\theta  \ge 1$ Show $\frac{d}{dx}(\tan x) = \sec^2 x$ , $\frac{d}{dx}(\sec x) = \sec x \tan x$ $\frac{d}{dx}(\cos ecx) = -\cos ecx \cot x$ , $\frac{d}{dx}(\cot x) = -\cos ec^2 x$	Page 40 Ex 7 Qu 1, 2, 3a,c,e,g, 4a	Page 18 Ex 6 Qu 1-4
6	Remind about Exponential function $f(x) = a^x$ (and $e^x$ ) Differentiate from 1st P => $f'(e^x) = e^x$ use spreadsheet to show $\lim_{h\to 0} \frac{e^h - 1}{h} = 1$ Prove also that $\frac{d}{dx}(\ln x) = \frac{1}{x}$	Page 43 Ex 8A Qu 1a,c,e, 2a, 3e 4a-c, 5b,d, 6a,d	$f(x) = e^{2x}, e^{x^2}$ $x^2 e^x, e^{\sin x}$
7	Go over $\frac{d}{dx}(\ln 2x)$ , $\frac{d}{dx}(\ln x^2)$ , $\frac{d}{dx}(\ln(\cos x))$ Remind $e^{\ln x} = \ln(e^x) = x$	Page 43, Ex 8A Qu 1b,d 2b,c,d 3a,b,c 4d,e 5a,c,e 6b,c,e (If time => Ex 4B Qu 1)	Page 18, Ex 6
8.	Define $\frac{d^2y}{dx^2}$ , $\frac{d^3y}{dx^3}$ , $\frac{d^4y}{dx^4}$ , $f''(x)$ , $f'''(x)$ etc. 2nd derivative test for nature of stationary points	Page 46 Ex 9A Qu 1, 2, 3, 4, 6	
9.	Review Cumulative total = 22 periods		



# Applications of Differential Calculus (5/6 pers)

Mathematics 1 Outcome 2b

Pd	Lesson, Outline, Approach etc.	Nelson MIA - AH M1	TeeJay Publishers
1/2	Go over x (displacement) (s in Physics) $v = \frac{dx}{dt}$ = speed (velocity) $a = \frac{dv}{dt}$ = $\frac{d^2x}{dt^2}$ = acceleration	Page 51 Ex 1 Qu 1a, b, d, f, 2a, c, e 3, 4, 6, 7, 8, 10, 12	Page 20 Ex 7
	Home exercise 1 on all topics to date		
3/4	Go over "local maxima/minima" Don't go into in anything like depth of MIA Book Cover "split domain" functions (piece-wise) Basically find max / min in a closed interval (a, b] etc Study (i) local max/min, (ii) end points (not "a" above) and (iii) "critical points" and 2nd derivative test (where appropriate) for nature. (pg56)	Page 56 Ex 2 Qu 1, 3 a,c,e,g,i page 60 Ex 3 Qu 1 a,c,e, 5 a-d	Page 24 Ex 8
5	Optimisation - as for Fifth Year work with new differentiable functions Chose examples carefully from Nelson	Page 63 Ex 4A Choose 5 or 6 examples from Ex 4A/4B (hard)	Page 25 Ex 9
6	Review		
	Cumulative total = 28 periods		



## Integral Calculus (10/11 periods)

Mathematics 1 Outcome 3

Pd	Lesson, Outline, Approach etc.	Nelson MIA - AH M1	TeeJay Publishers
1	Go over idea of "anti-derivative" and area under a curve (See page 69 for explanation of area)	Page 70 Ex 1A and 1B	Page 29 Ex 1
	+ special rule for integration:- $\int (ax + b)^n dx = etc.$		
2	$\int e^{x} dx = e^{x} + c,  \int \frac{1}{x} dx = \ln x + c,  \int \sec^{2} x dx = \tan x + c$ $\int e^{ax+b} dx = \frac{1}{a} e^{ax+b} + c,  \int \frac{1}{ax+b} dx = \frac{1}{a} \ln(ax+b) + c \text{ etc}$	Page 72 Ex 2A + some of 2B if time	Page 31 Ex 2 Page 33 Ex 3 (some)
3.	Integration by substitution Simple ones by inspection More complicated - substitution will be given Go over :- $\int 4x(x^2 + 5)dx$ , $\int 12x^2\sqrt{x^3 - 5}dx$ , $\int 4\sin x \cos^3 x dx$	page 74 Ex 3 Qu's - odd numbers	Page 36 Ex 4
4	Integration by Substitution part 2 - substitutions given Go over $\int \frac{\ln x}{x} dx$ , given $u = \ln x$ Go over $\int \sqrt{4 - x^2} dx$ , given $x = 2\sin u$ and $dx = 2\cos u du$	Page 75 Ex 4A Qu's - Odd Numbers	Page 37 Ex 5 Page 38 Ex 6
5	Show $\int \sin^5 x dx = \int \sin x \sin^4 x dx = \int \sin x (1 - \cos^2 x)^2 dx$ 2nd half of period go over definite integration and changing the limits for the new variables.	Page 76 Ex 4B Qu 1-5 Page 77 Ex 5A odd no's +1 or 2 from Ex 5B	
6	Special case $\int \frac{f'(x)}{f(x)} dx = \ln f(x)  + c$ Go over $\int \frac{x^2}{x^3 - 1} dx$ , $\int \frac{e^{3x}}{e^{3x} + 1} dx$ , $\int \tan x dx$ etc	page 80 Ex 6A Qu 1 c,d, 10 + few more Some of Ex 6B if time	
7	Areas under curves and between curves (rev <sup>n</sup> of 55 work)		Page 40 Ex 7 Page 41 Ex 8
8	Areas between curves and y -axis		page 42 Ex 9
9	Volumes of solids of revolution	Page 89 Qu 4, 5, 10	Page 44 Ex 10
10	Go over motion :- $\int a(t)dt = v(t)$ and $\int v(t)dt = x(t)$ See examples on page 88	Page 88 Ex 10A Qu 1, 2, 4, 6, 7, 8 (Rest of Ex 10A + some of Ex 10B if time)	
11	Review		
	Cumulative total = 39 periods		



## Functions and Graphs (6/7 pers)-Graphics Calc<sup>S</sup>

Mathematics 1 Outcome 4

Pd	Lesson, Outline, Approach etc.	Nelson MIA - AH M1	TeeJay Publishers
1	Revise Function work from Higher + go over inverse function and how to find $f^{-1}$ . Show also related graphs of inverses	Page 97 Ex 1 orally Page 100 Ex 3 Qu 1 a,e,g,h 2 e,c,g + 3	
2	Inverse Trig Functions $y = \sin^{-1} x$ etc Go over graphs of $\cos^{-1} x$ , $\tan^{-1} x$ , $e^{x}$ , $ f(x) $ & domains Go over EVEN and ODD functions	Page 102 Ex 2 Qu 1 & 2 Page 99 Ex 1 Qu 2, 5, 6, 7 Page 108 Ex 8 Qu 3	page 68 Qu 1 Page 68 Qu 5
3	Vertical asymptotes of rational functions $f(x) = \frac{g(x)}{h(x)}$ V.A. occurs at $x = a$ if $h(a) = 0$ Discuss what happens as $x \rightarrow a^+$ and $a^-$ . Remind to divide if deg $g(x) \ge \deg h(x)$	Page 109 Ex 9 Qu 1	Page 50 Ex 1
4	Horizontal asymptotes if deg $g(x) \le \deg h(x)$ and sloping asymptotes if deg $g(x) = \deg h(x) + 1$	Page 110 Ex 10 Qu 1 a, b, g, f, k, l	Page 52 Ex 2
5	Sketch graphs of <i>f</i> (x) using V.A, H.A. S.A, T.Pt, Roots and y-intercept	Page 112 Ex 11 Qu 1 a, c, e, g, i, k, m	page 57 Ex 3
6	Related Graphs - from $f(x)$ , sketch $f(x - a) af(x) f(ax)$ $f(x) + a$ , $f'(x)$ , $f^{-1}(x)$ etc	Page 114 Ex 12A Select carefully from Page 117	Page 68 Ex 3
7	Review		
	Cumulative total = 46 periods		

# Matrices - Systems of Equations (4/5 pers)

Mathematics 1 Outcome 5

Pd	Lesson, Outline, Approach etc.	Nelson MIA - AH M1	TeeJay Publishers
	Some of the Matrix work from Maths 3 can be incorporated in this chapter if you wish to save time later e.g. inverse of a 2 x 2 matrix, det A and inverse of a 3 x 3		
1/2	Define a matrix, element, order, transpose etc Solve a system of equations $(2 \times 2 \text{ and } 3 \times 3)$ in matrix form by row operations to reduce :- $\begin{bmatrix} a & b & c & n \\ d & e & f & p \\ g & h & i & q \end{bmatrix} \text{ to } \begin{bmatrix} a & b & c & n \\ 0 & j & k & r \\ 0 & 0 & m & s \end{bmatrix}$ and hence find the solution Gaussian Elimination - Augmented form etc	Page 127 Ex 4A Qu 1 and 2	Page 78 Ex 1
3	Show that some systems have infinite solutions and some have none e.g. x + y + z = 6 $x + y + z = 62x + y - 2z = -2$ $2x + y - 2z = -23x + 2y - z = 4$ $3x + 2y - z = 3(infinite set) (no solns - inconsistent)$	page 130 Ex 5 Qu 1 a - c, 2	
4	Ill Conditioning (occurs when small change in value of a coefficient(s) results in large change in solution.	Page 137 Qu 2	page 79 Ex 2
5	Review		
	For Session 2001-2002		
	End of Mathematics 1		
	Cumulative total = 51 periods		
	Assuming 5 periods per week and 2 weeks in June, this unit should end around Thursday 31st October.		
	<pre>=&gt;3 periods revision (including specimen NAB3) + 1 period for test = 55 periods</pre>		
	TEST around Friday 2nd November Actua	al Test Date =	