## M $\alpha$ thematics

# National 5 Practice Paper C 

## Paper 1

Duration - 1 hour
Total marks - 40

- You may NOT use a calculator
- Attempt all the questions.
- Use blue or black ink.
- Full credit will only be given to solutions which contain appropriate working.
- State the units for your answer where appropriate.

The roots of are

$$
a x^{2}+b x+c=0 \quad x=\frac{-b \pm \sqrt{b^{2}-4 a c}}{2 a}
$$

Sine rule:

$$
\frac{a}{\sin A}=\frac{b}{\sin B}=\frac{c}{\sin C}
$$

Cosine rule:

$$
a^{2}=b^{2}+c^{2}-2 b c \cos A \quad \text { or } \quad \cos A=\frac{b^{2}+c^{2}-a^{2}}{2 b c}
$$

Area of a triangle: $\quad A=\frac{1}{2} a b \sin C$

Volume of a Sphere: $\quad V=\frac{4}{3} \pi r^{3}$

Volume of a cone:

$$
V=\frac{1}{3} \pi r^{2} h
$$

Volume of a pyramid:

$$
V=\frac{1}{3} A h
$$

Standard deviation: $\quad s=\sqrt{\frac{\sum(x-\bar{x})^{2}}{n-1}}=\sqrt{\frac{\sum x^{2}-\left(\sum x\right)^{2} / n}{n-1}}$, where $n$ is the sample size.
2. Evaluate $\frac{2}{7}\left(1 \frac{3}{4}+\frac{3}{8}\right)$.
3. Simplify $3(2 x-4)-4(3 x+1)$
4.

$$
f(x)=7-4 x
$$

(a) Evaluate $f(-2)$. 1
(b) Given that $f(t)=9$, find $t$.
5. Solve, by factorising

$$
7+6 x-x^{2}=0
$$

6. A hotel books taxis from a company called Quick-Cars.

The receptionist notes the waiting time for every taxi ordered over a period of two weeks. These times, in minutes, are shown below.

| 12 | 25 | 29 | 37 | 6 | 13 | 26 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 32 | 42 | 7 | 14 | 29 | 35 | 44 |

(a) For the given data, calculate:
(i) the median 1
(ii) the lower quartile 1
(iii) the upper quartile 1
(b) Calculate the interquartile range. 1

In another two week period, the hotel books taxis from a company called Fast-Cabs.
The median waiting time for Fast-Cabs is found to be 27.5 minutes and the interquartile range for Fast-Cabs is found to be 5 minutes.
(c) Use this information to compare the two companies.
7. Part of the graph of $y=\operatorname{asin}(x+b)^{\circ}$ is shown in the diagram.


State the values of $a$ and $b$.
8. In the diagram below, $A$ is the point $(-1,-7)$ and $B$ is the point $(4,3)$.

(a) Find the gradient of the line $A B$.
(b) $\quad \mathrm{AB}$ cuts the $y$-axis at the point $(0,-5)$.

Write down the equation of the line $A B$.
(c) The point $(3 k, k)$ lies on AB . Find the value of $k$.
9.

$$
f(x)=x^{2}+6 x-7
$$

(a) Write $f(x)$ in the form $(x+a)^{2}+b$.
(b) State the coordinates of the turning point of $f(x)$.
10. Andrew and Daisy each book in at the Sleepwell Lodge.
(a) Andrew stays for 3 nights and has breakfast on 2 mornings. His bill is £ 145 .
Write down an algebraic equation to illustrate this information.
(b) Daisy stays for 5 nights and has breakfast on 3 mornings. Her bill is $£ 240$.
Write down an algebraic equation to illustrate this information.
(c) Find the cost of one breakfast
11. (a) Evaluate $8^{\frac{2}{3}}$
(b) $\begin{array}{ll}\text { Simplify } & \frac{\sqrt{24}}{\sqrt{2}}\end{array}$
(c) Simplify $\frac{2 x+2}{(x+1)^{2}}$

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# National 5 Practice Paper C 

## Paper 2

Duration - 1 hour and 30 minutes
Total marks - 50

- You may use a calculator
- Attempt all the questions.
- Use blue or black ink.
- Full credit will only be given to solutions which contain appropriate working.
- State the units for your answer where appropriate.

1. Bacteria in a test-tube increase at the rate of $0.6 \%$ per hour. At 12 noon, there are 5000 bacteria.
At 3 pm , how many bacteria will be present?
Give your answer correct to 3 significant figures.
2. 



The tangent, $M N$, touches the circle, centre 0 , at L .
Angle JLN $=47^{\circ}$
Angle KPL $=31^{\circ}$
Find the size of angle KLJ.
3. Change the subject of the formula

$$
y=a x^{2}+c \quad \text { to } x
$$

4. A mug is in the shape of a cylinder with diameter 10 centimetres and height 14 centimetres.

(a) Calculate the volume of the mug.
(b) 600 millilitres of coffee are poured in.

Calculate the depth of the coffee in the mug.
5. The diagram below shows a big wheel at the fairground.


The wheel has 16 chairs equally spaced on its circumference.
The radius of the wheel is 9 metres.
As the wheel rotates in an anticlockwise direction, find the distance a chair travels in moving from position T to position P in the diagram.
6. Find the roots of the equation

$$
2 x^{2}+4 x-9=0
$$

Give your answers correct to one decimal place.
7. Two perfume bottles are mathematically similar in shape.


The smaller one is 6 centimetres high and holds 30 millilitres of perfume. The larger one is 9 centimetres high.

What volume of perfume will the larger one hold?
9. Determine the nature of the roots of the equation

$$
\begin{equation*}
(x-2)^{2}-5=0 \tag{4}
\end{equation*}
$$

10. A sheep shelter is part of a cylinder as shown in figure 1.

It is 6 metres wide and 2 metres high.


Figure 1
The cross-section of the shelter is a segment of a circle with centre 0 , as shown in figure 2 .

OB is the radius of the circle.


Figure 2

Calculate the length of OB.
11. The sketch shows a parallelogram, PQRS.

(a) Calculate the size of angle PQR. Do not use a scale drawing.
(b) Calculate the area of the parallelogram.
12. (a) Solve the equation

$$
\begin{equation*}
2 \tan x^{\circ}+7=0, \quad 0 \leq x \leq 360 \tag{3}
\end{equation*}
$$

(b) Prove that

$$
\sin ^{3} x+\sin x \cos ^{2} x=\sin x
$$

13. (a) A driver travels from $A$ to $B$, a distance of $x$ miles, at a constant speed of 75 kilometres per hour.

Find the time taken for this journey in terms of $x$.
(b) The time taken for the journey from $B$ to $A$ is $\frac{x}{50}$ hours.

Calculate the average speed for the whole journey.

