

# $M\alpha$ thematics

### National 5 Practice Paper C

Paper 1

Duration - 1 hour

Total marks - 40

- o You may NOT use a calculator
- Attempt all the questions.
- Use blue or black ink.
- o Full credit will only be given to solutions which contain appropriate working.
- o State the units for your answer where appropriate.

#### FORMULAE LIST

$$ax^2 + bx + c = 0$$
  $x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$ 

$$\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$$

$$a^2 = b^2 + c^2 - 2bc \cos A$$
 or  $\cos A = \frac{b^2 + c^2 - a^2}{2bc}$ 

$$A = \frac{1}{2}ab\sin C$$

$$V = \frac{4}{3}\pi r^3$$

$$V = \frac{1}{3}\pi r^2 h$$

$$V = \frac{1}{3}Ah$$

$$s=\sqrt{rac{\sum (x-ar{x})^2}{n-1}}=\sqrt{rac{\sum x^2-(\sum x)^2/n}{n-1}}$$
 , where  $n$  is the sample size.

$$5.04 + 8.4 \div 7$$
.

$$\frac{2}{7}\left(1\frac{3}{4}+\frac{3}{8}\right).$$

$$3(2x-4)-4(3x+1)$$

$$f(x) = 7 - 4x$$

(a) Evaluate 
$$f(-2)$$
.

(b) Given that 
$$f(t) = 9$$
, find  $t$ .

### 5. Solve, by factorising

$$7 + 6x - x^2 = 0.$$

6. A hotel books taxis from a company called Quick-Cars.

The recentionist notes the waiting time for every taxi ordered every

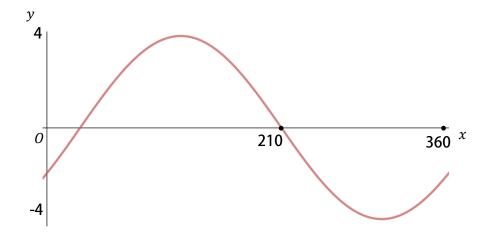
The receptionist notes the waiting time for every taxi ordered over a period of two weeks. These times, in minutes, are shown below.

- (a) For the given data, calculate:
  - (i) the median
  - (ii) the lower quartile 1
  - (iii) the upper quartile 1
- (b) Calculate the interquartile range.

In another two week period, the hotel books taxis from a company called Fast-Cabs.

The median waiting time for Fast-Cabs is found to be 27.5 minutes and the interquartile range for Fast-Cabs is found to be 5 minutes.

- (c) Use this information to compare the two companies.
- 7. Part of the graph of  $y = a\sin(x + b)^{\circ}$  is shown in the diagram.

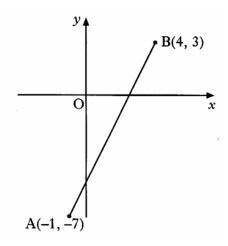


State the values of a and b.

1

1

8. In the diagram below, A is the point (-1, -7) and B is the point (4,3).



(a) Find the gradient of the line AB.

1

(b) AB cuts the y-axis at the point (0,-5). Write down the equation of the line AB.

2

2

(c) The point (3k, k) lies on AB. Find the value of k.

- 9.  $f(x) = x^2 + 6x 7$ 
  - (a) Write f(x) in the form  $(x + a)^2 + b$ .

2

(b) State the coordinates of the turning point of f(x).

10.	Andrew and Daisy each book in at the Sleepwell Lodge.				
	(a)	3 nights and has breakfast on 2 mornings.  Igebraic equation to illustrate this information.	1		
	(b)	Her bill is £240.	nights and has breakfast on 3 mornings.  lgebraic equation to illustrate this information.	1	
	(c)	Find the cost of	one breakfast	3	
11.	(a)	Evaluate	$8^{\frac{2}{3}}$	2	
	(b)	Simplify	$\frac{\sqrt{24}}{\sqrt{2}}$	2	
	(c)	Simplify	$\frac{2x+2}{(x+1)^2}$	2	

[End of question paper]



# $M\alpha$ thematics

### National 5 Practice Paper C

Paper 2

Duration - 1 hour and 30 minutes

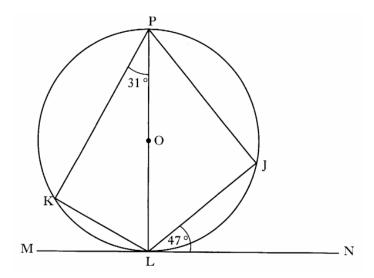
Total marks - 50

- o You may use a calculator
- Attempt all the questions.
- Use blue or black ink.
- o Full credit will only be given to solutions which contain appropriate working.
- o State the units for your answer where appropriate.

Bacteria in a test-tube increase at the rate of 0.6% per hour.
 At 12 noon, there are 5000 bacteria.
 At 3 pm, how many bacteria will be present?
 Give your answer correct to 3 significant figures.

4

2.



The tangent, MN, touches the circle, centre O, at L.

Angle JLN =  $47^{\circ}$ 

Angle KPL = 31°

Find the size of angle KLJ.

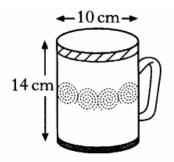
3

3. Change the subject of the formula

$$y = ax^2 + c$$

to 
$$x$$
.

4. A mug is in the shape of a cylinder with diameter 10 centimetres and height 14 centimetres.



2

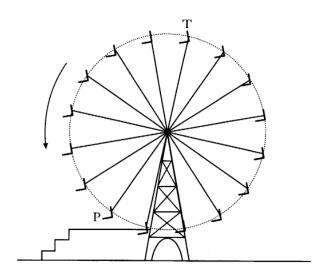
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4

- (a) Calculate the volume of the mug.
- (b) 600 millilitres of coffee are poured in.

Calculate the depth of the coffee in the mug.

5. The diagram below shows a big wheel at the fairground.



The wheel has 16 chairs equally spaced on its circumference. The radius of the wheel is 9 metres.

As the wheel rotates in an anticlockwise direction, find the distance a chair travels in moving from position T to position P in the diagram.

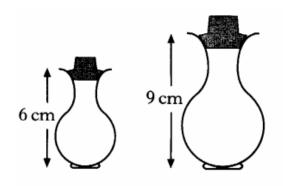
6. Find the roots of the equation

$$2x^2 + 4x - 9 = 0,$$

Give your answers correct to one decimal place.

4

7. Two perfume bottles are mathematically similar in shape.



The smaller one is 6 centimetres high and holds 30 millilitres of perfume. The larger one is 9 centimetres high.

What volume of perfume will the larger one hold?

3

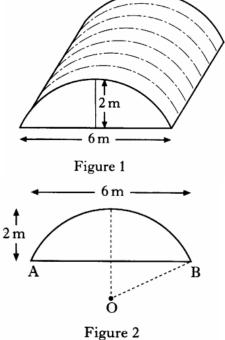
9. Determine the nature of the roots of the equation

$$(x-2)^2 - 5 = 0.$$

10. A sheep shelter is part of a cylinder as shown in figure 1.

> It is 6 metres wide and 2 metres high.

The cross-section of the shelter is a segment of a circle with centre O, as shown in figure 2.



4

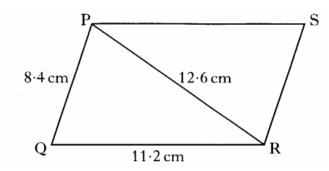
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3

OB is the radius of the circle.

Calculate the length of OB.

The sketch shows a parallelogram, PQRS. 11.



- Calculate the size of angle PQR. Do not use a scale drawing. (a)
- Calculate the area of the parallelogram. (b)

12.	(a)	Solve the	
1/	(2)	ZOIVE THE	eanana

$$2 \tan x^{\circ} + 7 = 0$$
,  $0 \le x \le 360$ .

$$0 < x < 360$$
.

3

(b) Prove that

$$\sin^3 x + \sin x \cos^2 x = \sin x.$$

2

A driver travels from A to B, a distance of x miles, at a constant speed 13. (a) of 75 kilometres per hour.

Find the time taken for this journey in terms of x.

1

The time taken for the journey from B to A is  $\frac{x}{50}$  hours. (b)

Calculate the average speed for the whole journey.

4

[End of question paper]